compute_cstat_gof

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How to compute cstat goodness of fit in CIAO/Sherpa Vinay Kashyap (CXC/CfA)

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This is a walkthrough of a python script written by Long Xi, translated from an IDL script written by Vinay Kashyap, based on piecewise approximation of the nominal cstat prescribed by Kaastra (2017, A&A, 605, A51).

It computes the *expected* cstat and the *expected* variance in the cstat for the best-fit model, and compares it to the cstat computed for the observed data and the best-fit model. If the observed cstat is significantly higher than the estimated cstat, the model is likely a bad fit. If it is significantly smaller, it is an indication that the data are being *overfit*.

It requires the sherpa.astro.ui and scipy packages. The example uses an ACIS-S dataset of Quasar Q1127-145, ObsID 866 that has been previously used to demo pyBLoCXS.

This notebook, as well as the cstat_gof.py script, and all the associated data files used here, are available on the IACHEC website.

Initialize packages

```
[1]: from sherpa.astro.ui import *
   from glob import glob
   import numpy as np
   from scipy.special import factorial
```

Load in the cstat goodness-of-fit calculator script This is available within the associated tar file as cstat/cstat_gof.py

[2]: import cstat_gof

Load in example dataset Set the energy range to

Set the energy range to be extremely large, because we want to demonstrate what happens with a *bad fit* first.

```
[3]: load_data("obs866/acis.pi")
    ignore()
    notice(0.1,10)
```

read ARF file obs866/acis.arf
read RMF file obs866/acis.rmf
read background file obs866/acis_bg.pi

Define a model

Again, because we want to demonstrate a bad fit, let us pick a model that is clearly inappropriate for a Quasar spectrum. We will assume an optically thin thermal emission model with no absorption.

```
[4]: set_model(xsapec.kT1)
```

```
Set the statistic to cstat
[5]: set_stat('cstat')
```

Fit the model to the data [6]: fit()

```
WARNING: data set 1 has associated backgrounds, but they have not been
subtracted, nor have background models been set
Dataset
                     = 1
Method
                     = levmar
Statistic
                     = cstat
Initial fit statistic = 5.72125e+07
Final fit statistic = 3273.77 at function evaluation 141
Data points
                     = 679
                     = 677
Degrees of freedom
Probability [Q-value] = 0
Reduced statistic
                     = 4.83571
Change in statistic
                     = 5.72092e+07
  kT1.kT
                              +/- 11.2441
                 64
                 0.00274832 +/- 0.000143993
  kT1.norm
WARNING: parameter value kT1.kT is at its maximum boundary 64.0
```

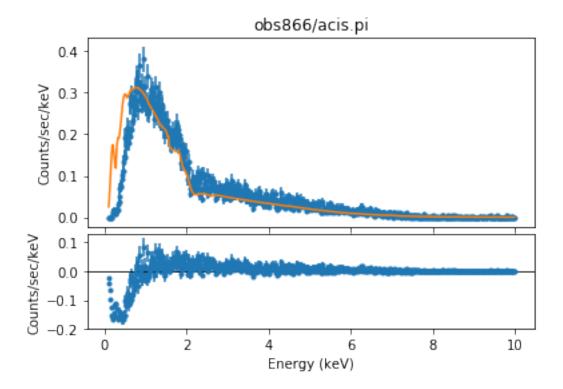
Show the fit

Notice that the fit is obviously bad, with large residuals at low energies that contributes to a large cstat value. If this were a chisq fit, we would say reduced chisq = 4.8

```
[7]: plot_fit_resid()
    calc_stat_info()
    obscstat = calc_stat()
    print("observed cstat = ",obscstat)
```

```
WARNING: The displayed errorbars have been supplied with the data or calculated
using chi2xspecvar; the errors are not used in fits with cstat
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using chi2xspecvar; the errors are not used in fits with cstat
WARNING: data set 1 has associated backgrounds, but they have not been
subtracted, nor have background models been set
                     = 1
Dataset
Statistic
                     = cstat
Fit statistic value = 3273.77
Data points
                     = 679
Degrees of freedom = 677
Probability [Q-value] = 0
Reduced statistic = 4.83571
```

WARNING: data set 1 has associated backgrounds, but they have not been subtracted, nor have background models been set observed cstat = 3273.7730508449263



Compute expected cstat for best-fit model

Extract the energy array and the model values from the plot and call the cstat_gof script.

[8]: x = get_data_plot().x y = get_data_plot().y [Ce,Cv] = cstat_gof.gof_cstat(x,y) print("expected cstat = ",Ce," +- ",np.sqrt(Cv))

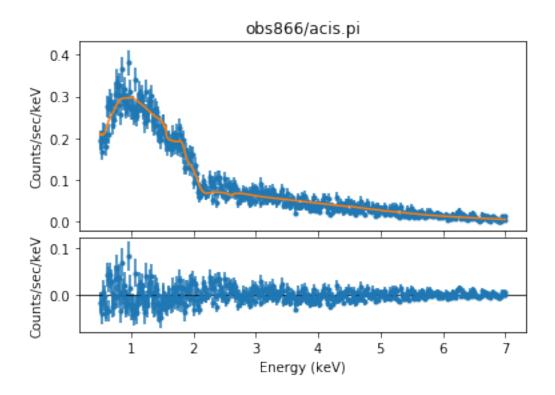
WARNING: The displayed errorbars have been supplied with the data or calculated using chi2xspecvar; the errors are not used in fits with cstat WARNING: The displayed errorbars have been supplied with the data or calculated using chi2xspecvar; the errors are not used in fits with cstat expected cstat = 713.980182016839 +- 37.46020112454112

Ce is the cstat value expected if the data were generated based on the model values (Eq 4 of Kaastra 2017).

Cv is the expected variance (Eq 6 of ibid). They are computed using the approximations given in Sec 3, ibid). *Evaluate goodness of fit*

```
[9]: print("how good is the fit?")
     qual = (obscstat-Ce)/np.sqrt(Cv)
     print("Observed cstat is off from expected by ",qual," sigma")
    how good is the fit?
    Observed cstat is off from expected by 68.33366591700178 sigma
       Whew, that is a very bad fit.
       Now let us see how a good fit behaves
       We will use a shorter energy range and a more realistic model (an absorbed power-law, natch)
[10]: ignore()
     notice(0.5,7.0)
     set_model(xstbabs.abs1*xspowerlaw.pl1)
     fit()
     plot_fit_resid()
     obscstat = calc_stat()
     print("observed cstat = ",obscstat)
    WARNING: data set 1 has associated backgrounds, but they have not been
    subtracted, nor have background models been set
    Dataset
                          = 1
    Method
                          = levmar
    Statistic
                          = cstat
    Initial fit statistic = 3.14697e+07
    Final fit statistic = 476.76 at function evaluation 32
    Data points
                          = 446
    Degrees of freedom = 443
    Probability [Q-value] = 0.129483
    Reduced statistic
                         = 1.07621
                          = 3.14692e+07
    Change in statistic
       abs1.nH
                      0.0707008
                                    +/- 0.00771314
                                    +/- 0.0239493
       pl1.PhoIndex 1.17661
                      0.000534254 +/- 1.35057e-05
       pl1.norm
    WARNING: The displayed errorbars have been supplied with the data or calculated
    using chi2xspecvar; the errors are not used in fits with cstat
    WARNING: The displayed errorbars have been supplied with the data or calculated
    using chi2xspecvar; the errors are not used in fits with cstat
    WARNING: data set 1 has associated backgrounds, but they have not been
    subtracted, nor have background models been set
```

observed cstat = 476.75951254247997



That seems like a good fit, cstat is 477 with 443 degrees of freedom. *How deviant is the fit?*

```
[11]: x = get_data_plot().x
```

```
y = get_data_plot().y
[Ce,Cv] = cstat_gof.gof_cstat(x,y)
print("expected cstat = ",Ce," +- ",np.sqrt(Cv))
print("how good is the fit?")
qual = (obscstat-Ce)/np.sqrt(Cv)
print("Observed cstat is off from expected by ",qual," sigma")
```

```
WARNING: The displayed errorbars have been supplied with the data or calculated
using chi2xspecvar; the errors are not used in fits with cstat
WARNING: The displayed errorbars have been supplied with the data or calculated
using chi2xspecvar; the errors are not used in fits with cstat
expected cstat = 481.93243579262844 +- 30.819214681479007
how good is the fit?
Observed cstat is off from expected by -0.16784734145926083 sigma
```

Observed cstat is off by about -0.2 sigma from the expected cstat. That is definitely a good fit!